Abstract: We're going to set out to find the square root of 2! Along the way we'll meet some of our oldest friends from calculus, invent non-existent eigenvectors, and ultimately completely abandon rationality to find ourselves facing open questions in algebraic number theory. This talk will be accessible to anyone who's ever taken Calculus I.